

Algebra 1 Sample Problems:

1. Combining fractions (add/subtract, multiply/divide, simplify)

Example 1:

- i. $1 + \frac{4}{9}$
- ii. $\left(\frac{9}{9}\right)1 + \frac{4}{9}$
- iii. $\frac{9+4}{9}$
- iv. $\frac{13}{9}$

Example 2:

- i. $\frac{1/\cancel{12}}{3/4}$
- ii. $\frac{1}{12} \cdot \frac{4}{3}$
- iii. $\frac{4}{36} = \frac{4}{4 \times 9}$
- iv. $\left(\frac{\cancel{4}}{\cancel{4}}\right)\frac{1}{9}$
- v. $\frac{1}{9}$

2. Converting from one linear form to another

Find the equation of the line that passes through (2,3) with a slope of -5

- i. $y - y_1 = m(x - x_1)$ Point-Slope Form
- ii. $y - 3 = -5(x - 2)$
- iii. $y - 3 = -5x + 10$
- iv. $y = -5x + 13$ Slope-Intercept Form
- v. $5x + y = 13$ Standard Form

3. Multiplying powers with like bases

Given:

- i. $x^2 \cdot x^{a-2}$
- ii. x^{2+a-2} Add exponents
- iii. x^a Simplify

4. Dividing powers with like bases

Given:	i.	$\frac{5^x}{5^{x+2}}$	
	ii.	$5^{x-(x+2)}$	Subtract exponents
	iii.	5^{x-x-2}	
	iv.	5^{-2}	Simplify
	v.	$\frac{1}{5^2}$	Simplify

5. Raising a product or a quotient to a power

Given:	i.	$(a^2b^3)^5$	
	ii.	$a^{2 \cdot 5}b^{3 \cdot 5}$	Multiply exponents
	iii.	$a^{10}b^{15}$	Simplify

6. Factoring trinomials

This example uses a trinomial where the lead coefficient is other than “1”. The method employed here is called the “bottoms up” method.

i.	$3x^2 + 10x - 8$	Given
ii.	$x^2 + 10x - 24$	Multiply the constant by the leading coefficient
iii.	$(x+12)(x-2)$	Factor as if the leading coefficient were “1”
iv.	$(x + \frac{12}{3})(x - \frac{2}{3})$	Divide the constants by the original coefficient
v.	$(x+4)(x - \frac{2}{3})$	Simplify each fraction.
vi.	$(x+4)(3x-2)$	Move any denominator for each binomial into the lead coefficient position. Check the resulting factors by using FOIL.

7. Simplifying complex rational expressions

i.	$\frac{x-2}{x-2} + \frac{x+2}{x^2-4}$
ii.	$\frac{x-2}{x-2} + \frac{x+2}{(x+2)(x-2)}$
iii.	$\left(\frac{x+2}{x+2}\right)\frac{x-2}{x-2} + \frac{x+2}{(x+2)(x-2)}$
iv.	$\frac{x^2-4+x+2}{(x+2)(x-2)}$

$$\text{v. } \frac{x^2 + x - 2}{(x+2)(x-2)}$$

$$\text{vi. } \frac{\cancel{(x+2)}(x-1)}{\cancel{(x+2)}(x-2)}$$

$$\text{vii. } \frac{x-1}{x-2}$$

8. Solving problems involving distance/rate/time

Example: A train leaves Sacramento at a speed of 60 kilometers per hour. Two hours later another train leaves Sacramento on a parallel track at 90 kilometers per hour. At what point will the second train catch up to the first train?

- a) Fill in the chart above with the correct information:

	DISTANCE	RATE	TIME
First Train	(the distance equals the distance below) or d	60	x
Second Train	(the distance equals the distance above) or d	90	$x-2$

- b) Since it is known that $d = rt$ (Distance = Rate x Time), the first train's distance will be equal to $d = 60x$. The second train's distance will be equal to $d = 90(x-2)$.
- c) $d = d$ because that is the distance where the second train catches the first train.
- d) Logically, if $d = d$, then substitute $60x$ and $90(x-2)$ for those values, or $60x = 90(x-2)$.
- e) Solve:
- i. $d = d$
 - ii. $60x = 90(x-2)$
 - iii. $60x = 90x - 180$
 - iv. $-30x = -180$
 - v. $x = 6$
- f) The first train will have traveled 6 hours at 60 miles per hour or 360 miles. The second train will have traveled 4 hours at 90 miles per hour or 360 miles.

9. Using the elimination method solve a linear system

Given:

i.	$2x + 5y = 8$	
	$x - 3y = 2$	
ii.	$2x + 5y = 8$	Multiply 2 nd equation by 2
	$2(x - 3y) = 2(2)$	
iii.	$2x + 5y = 8$	Subtract 2 nd equation from 1 st
	$2x - 6y = 4$	
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	$11y = 4$	
iv.	$y = \frac{4}{11}$	Solve for y

Now substitute into either equation to find x . . .

v.	$2x + 5\left(\frac{4}{11}\right) = 8$	
vi.	$2x + \frac{20}{11} = 8$	
vii.	$2x\left(\frac{11}{11}\right) + \frac{20}{11} = 8\left(\frac{11}{11}\right)$	Common denominator
viii.	$22x + 20 = 88$	
ix.	$22x = 68$	
x.	$x = \frac{68}{22} \text{ or } \frac{34}{11}$	

Check your answer.

10. Dividing radical expressions

Given:

i.	$\frac{\sqrt[3]{25a^2b^5}}{\sqrt[3]{5ab}}$
ii.	$\sqrt[3]{\frac{25a^2b^5}{5ab}}$
iii.	$\sqrt[3]{5a^{2-1}b^{5-1}}$
iv.	$\sqrt[3]{5ab^4}$
v.	$5^{1/3} a^{1/3} b^{4/3}$
vi.	$b^3\sqrt[3]{5ab}$

11. Rationalizing denominators

Given:

- i. $\frac{4}{\sqrt{3} + x}$
- ii. $\frac{4}{\sqrt{3} + x} \left(\frac{\sqrt{3} - x}{\sqrt{3} - x} \right)$
- iii. $\frac{4\sqrt{3} - 4x}{3 - x\sqrt{3} + x\sqrt{3} - x^2}$
- iv. $\frac{4\sqrt{3} - 4x}{3 - x^2}$

12. Graphing parabolas

Sketch $g(x) = 4x^2 + 8x - 3$

Change the quadratic equation to the $a(x - h)^2 + k = y$ form.

Part One:

- | | | |
|------|------------------------------|---|
| i. | $g(x) = 4x^2 + 8x - 3$ | Remember $g(x) = y$ |
| ii. | $4x^2 + 8x - 3 = 0$ | Make $y = 0$ |
| iii. | $4x^2 + 8x = 3$ | Add the constant term to both sides of the equation. |
| iv. | $4(x^2 + 2x + \dots) = 3$ | Factor out the 4, complete the square. |
| v. | $4(x^2 + 2x + 1) = 3 + 4(1)$ | Complete the square and add the right amount to both sides of the equation. |
| vi. | $4(x + 1)^2 = 7$ | Factor the trinomial and change to $a(x - h)^2 + k = y$ form. |
| vii. | $4(x + 1)^2 - 7 = 0$ | |

The a-value is a +4 so the direction of the parabola opens upward. The (h,k) is (-1,-7) so the vertex is in the third quadrant. There will be two x-intercepts.

Part Two:

To find x-intercepts. . .

i. $4(x+1)^2 - 7 = 0$

ii. $(x+1)^2 = \frac{7}{4}$

iii. $\sqrt{(x+1)^2} = \frac{\sqrt{7}}{\sqrt{4}}$

iv. $x+1 = \pm \frac{\sqrt{7}}{2}$

v. $x = +0.3$ or $x = -2$

To find x-intercepts, make $y = 0$.

Add +7 to both sides, divide by 4.

To “undo” a square, take the square root.

Remember the square root is plus/minus.

Subtract +1 from each side, estimate $\frac{\sqrt{7}}{2}$ and get the two roots.

To find the y-intercept. . .

i. $4(0+1)^2 - 7 = y$

ii. $4 - 7 = y$

iii. $-3 = y$

Make $x = 0$

Simplify

The parabola crosses the y-axis at $(0,-3)$.

Sketch the graph:

